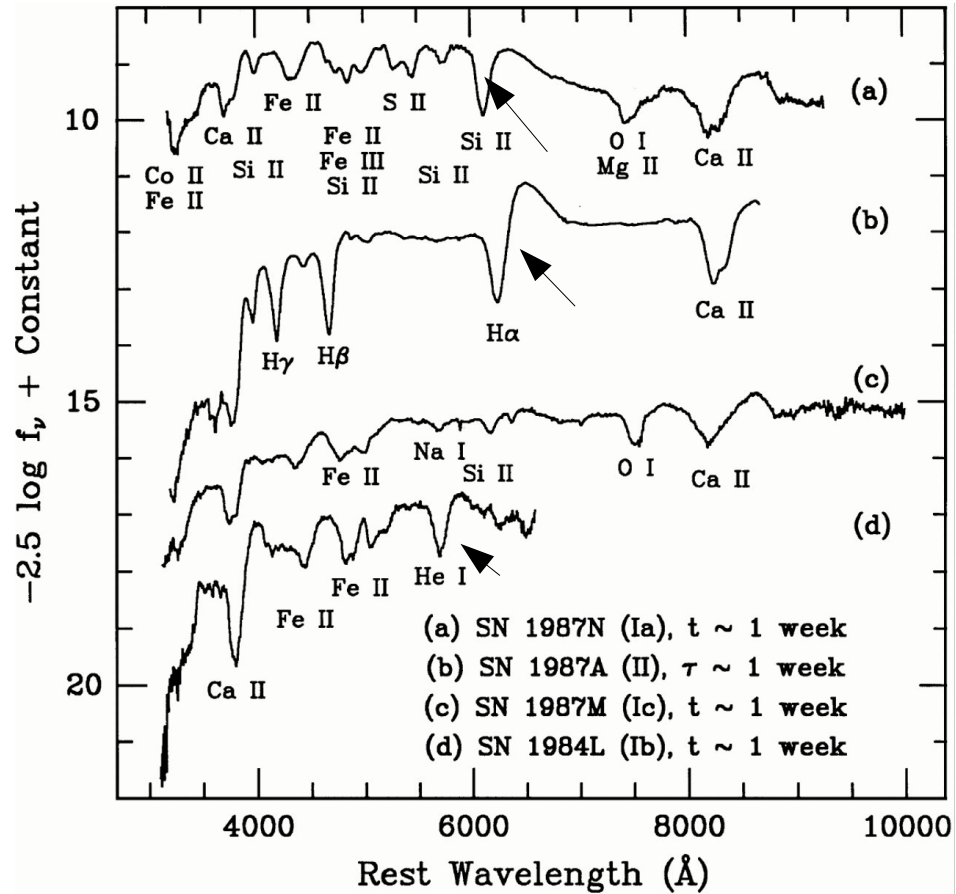


# SN classification

Early spectra



Type I: no H

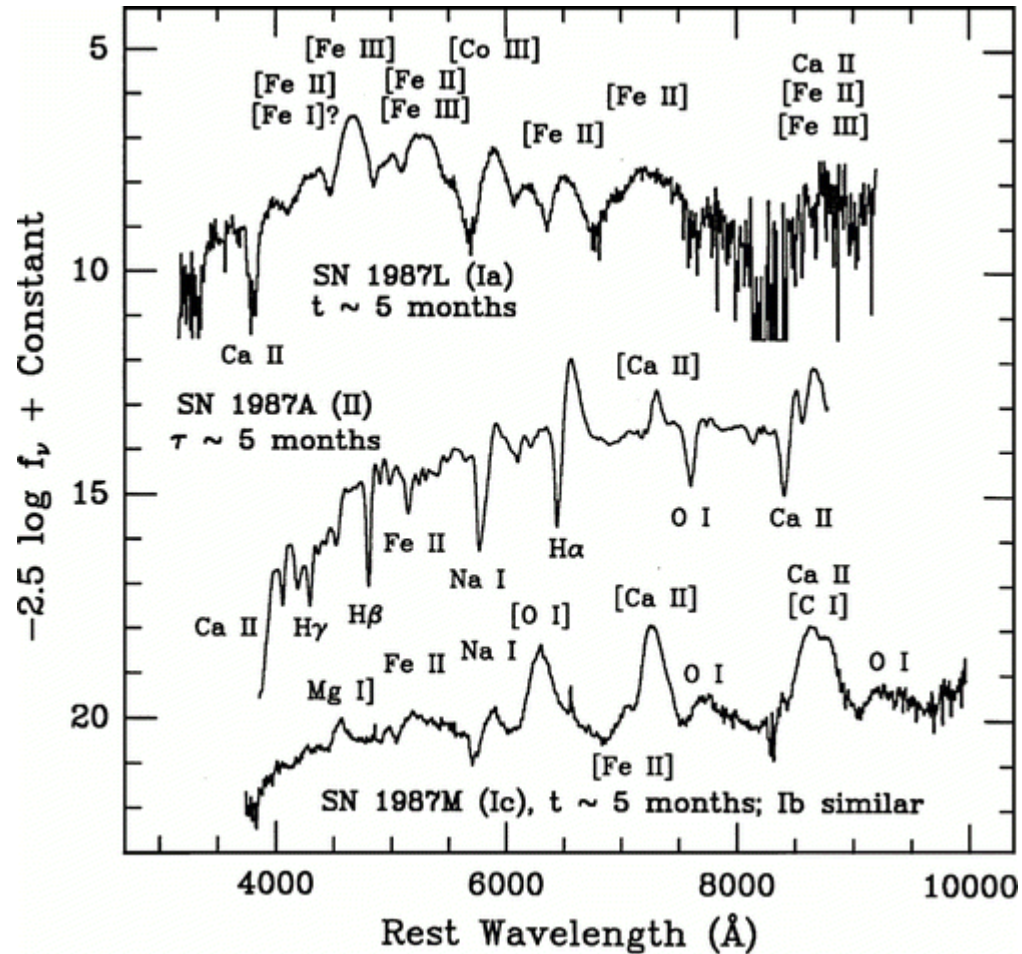
Type II: H

Ia: Si 6150 line      Ib/c no Si line

Ib He      Ic no He

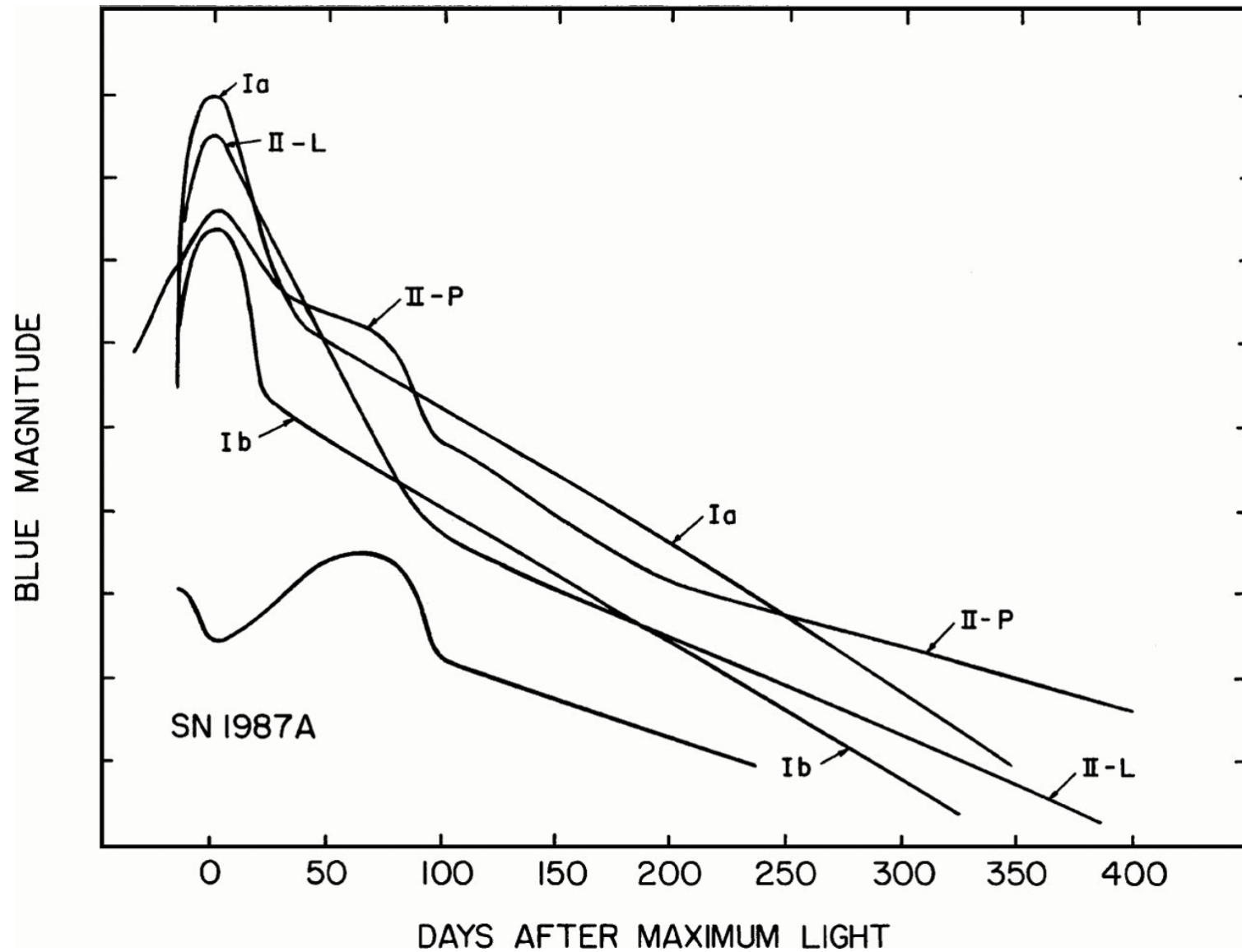


# Late spectra



Type Ia: Strong Fe II-III lines

Ib/c: strong O I, Ca II, Mg I



Type IIP: Plateau ~ 100 days IIL: Linear decline

# Shock break-out

$$E_{th} \approx E_{tot} / 2$$

$$\epsilon V = a T^4 \frac{4\pi}{3} R^3$$

$$T_{eff} \approx 2 \times 10^5 E_{51}^{1/4} R_{13}^{-3/4}$$

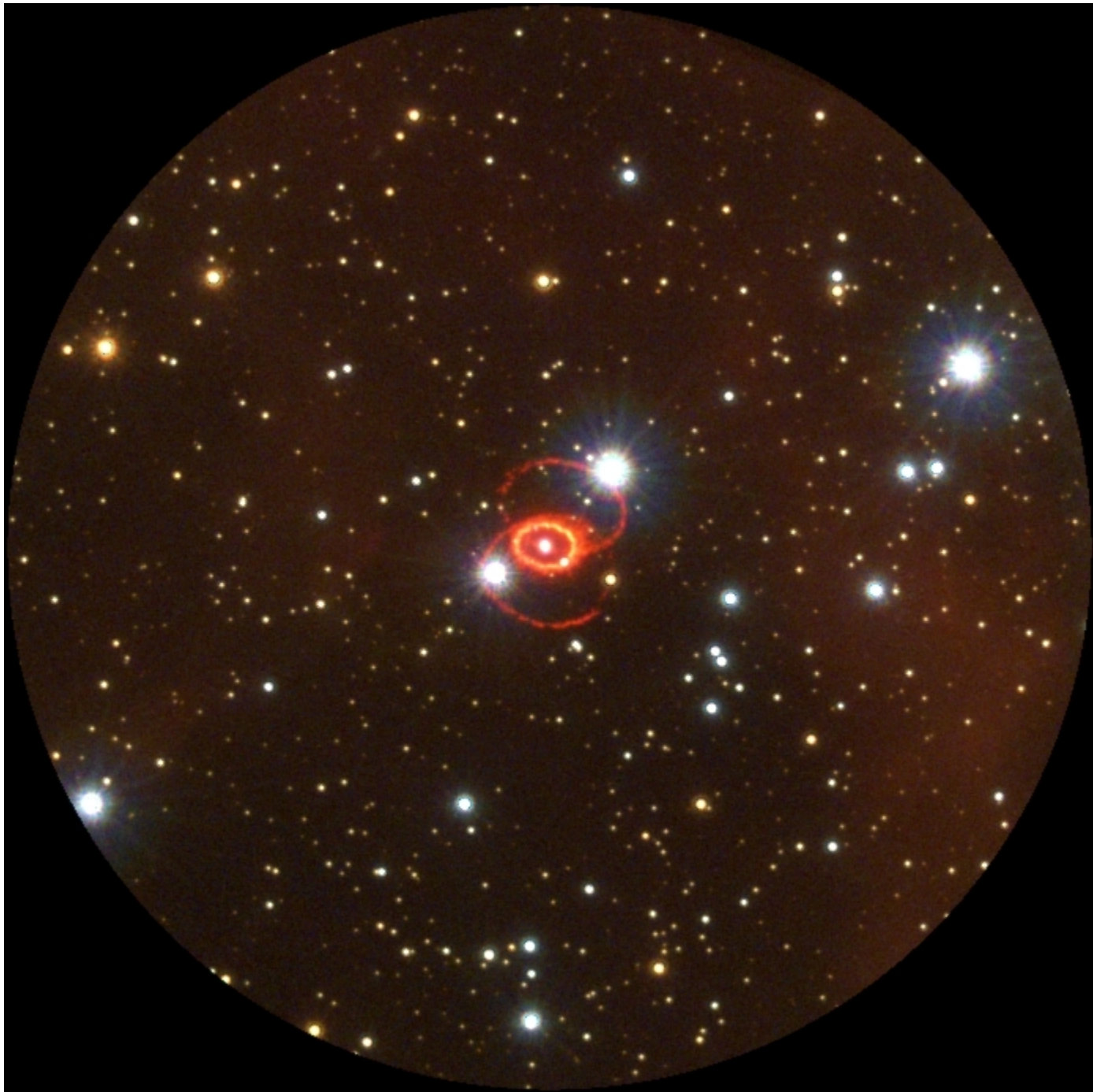
$$\text{Scatterings} \Rightarrow T_{color} \sim 2 T_{eff}$$

$$\text{RSG } R \sim 10^{13} - 10^{14} \text{ cm } T < 5 \times 10^4 \text{ K}$$

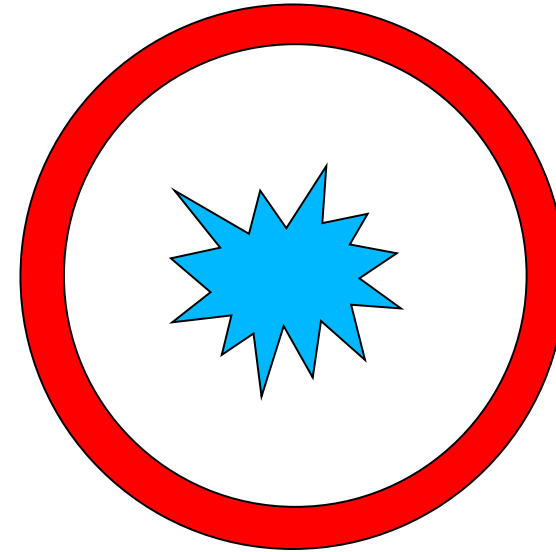
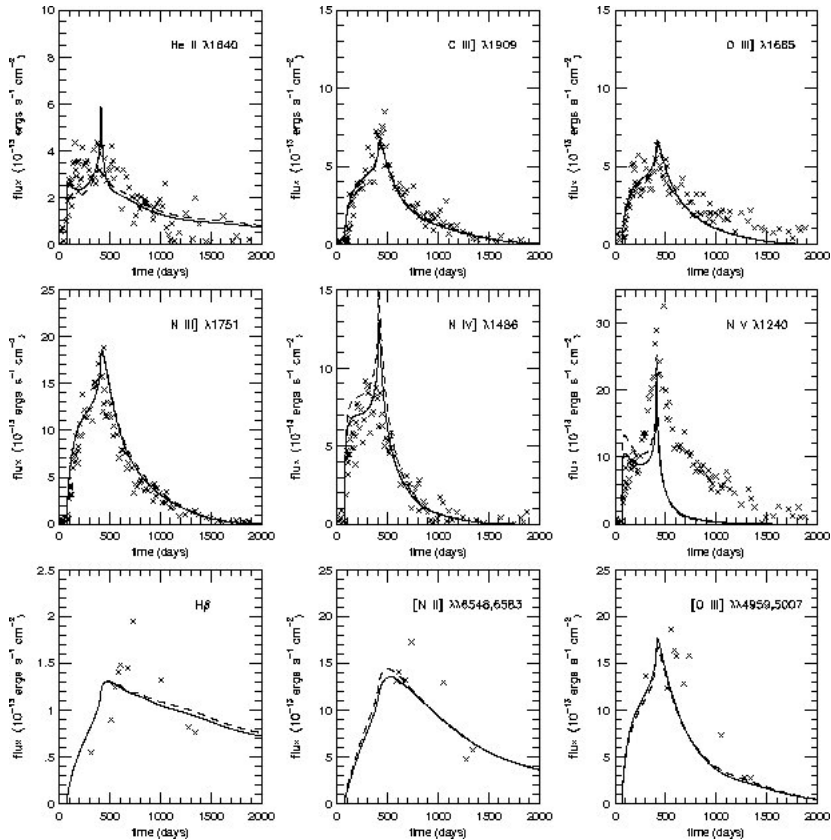
$$\text{WR } R \sim 10^{11} \text{ cm } \quad T \sim 5 \times 10^6 \text{ K}$$



# The Ring



# What makes the rings glow?



X-ray flash at shock breakout  
during first hour + recombination  
+ light echo of ring  
Radius  $\sim 190$  light days

P. Lundqvist + CF 96

# Shock break-out in SN 1987A

$$\text{BSG } R \sim 2 \times 10^{12} \text{ cm} \quad E \sim 1.5 \times 10^{51} \text{ ergs} \quad T_{\text{eff}} \sim 4 \times 10^5 \text{ K}$$

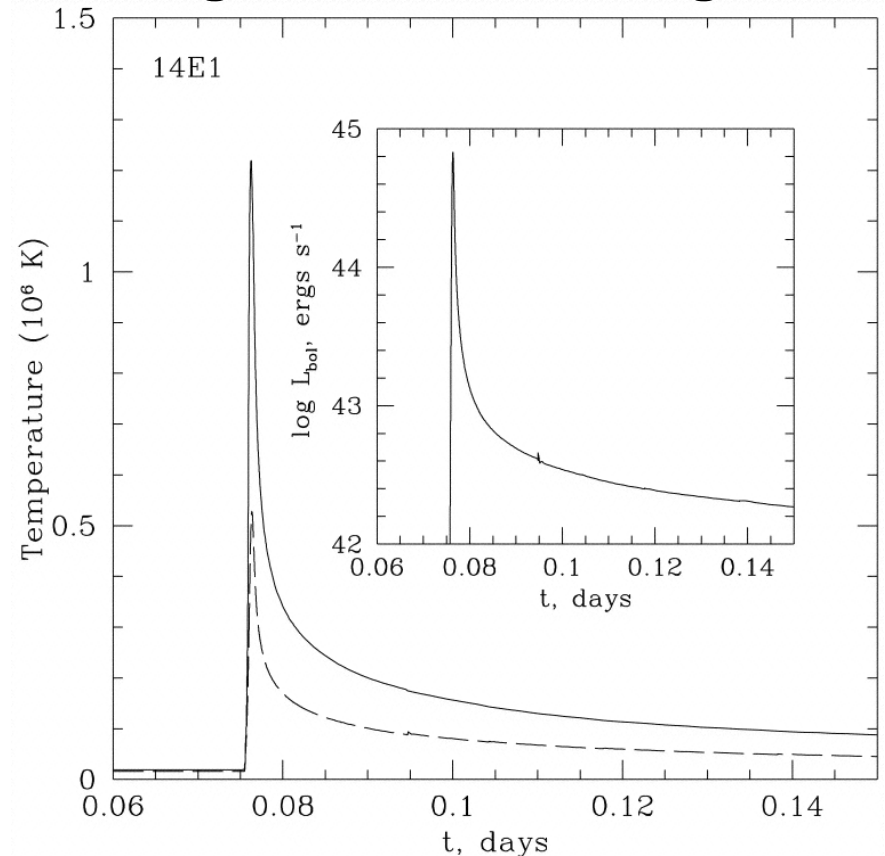
$$T_{\text{color}} \sim 10^6 \text{ K} \quad \tau \sim 3\text{-}4 \text{ min} \quad L \sim 10^{45} \text{ erg s}^{-1} \quad E \sim 10^{47} \text{ ergs}$$

Ionization and heating of rings of  
SN 1987A

Observe N III-N V

Needs  $T_{\text{color}} \sim 10^6 \text{ K}$  !

Break-out confirmed years later!





# Diffusion phase

$$t_{diff} \approx \frac{R^2 \rho \kappa}{3 \pi^2 c}$$

$$t_{exp} \approx \frac{R}{V}$$

$$\frac{t_{diff}}{t_{exp}} \approx 0.2 \frac{M}{M_{\odot}} \frac{V}{10^4 \text{ km s}^{-1}} \left( \frac{R^2}{10^{15} \text{ cm}} \right)^{-2}$$

$$M \sim 10 M_{\odot} \quad R_{\text{peak}} \sim 10^{15} \text{ cm}$$

Up to  $R_{\text{peak}}$  radiation is trapped  $\Rightarrow$  adiabatic expansion

from  $R_{\odot}$  to  $R_{\text{peak}}$

# Diffusion phase

$$E_{int} = (\gamma - 1) p V = \frac{1}{3} K \rho^{4/3} V \propto R^{-1}$$

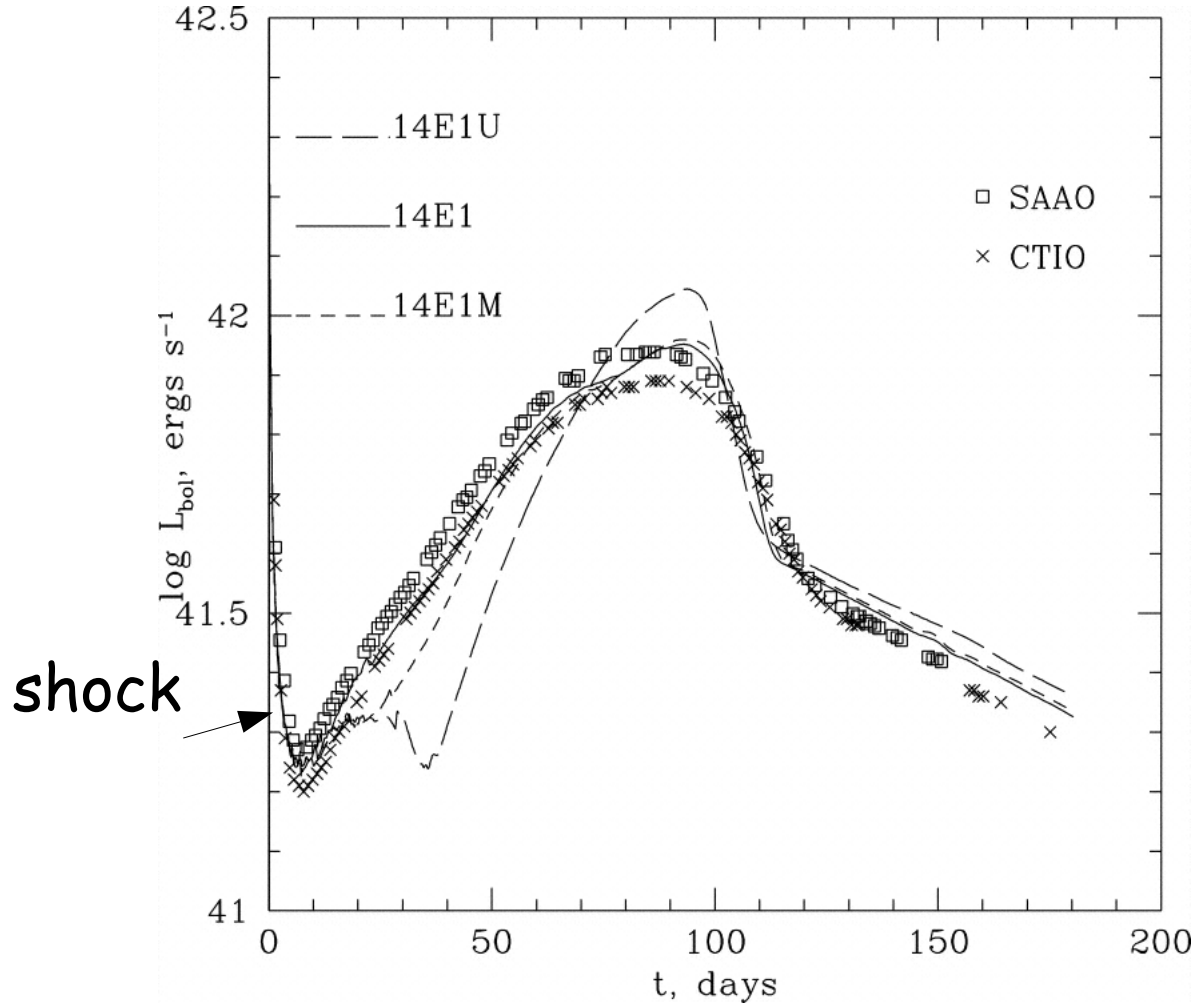
Small  $R_o \Rightarrow$  most internal energy lost in adiabatic expansion  $\Rightarrow$  faint SN!

RSG progenitors: Shock energy may power LC for  $\sim 100$  days

BSG progenitors, WR stars: Shock energy lost  
Need other energy source

# SN 1987A

progenitor BSG  $R \sim 10^{12}$  cm



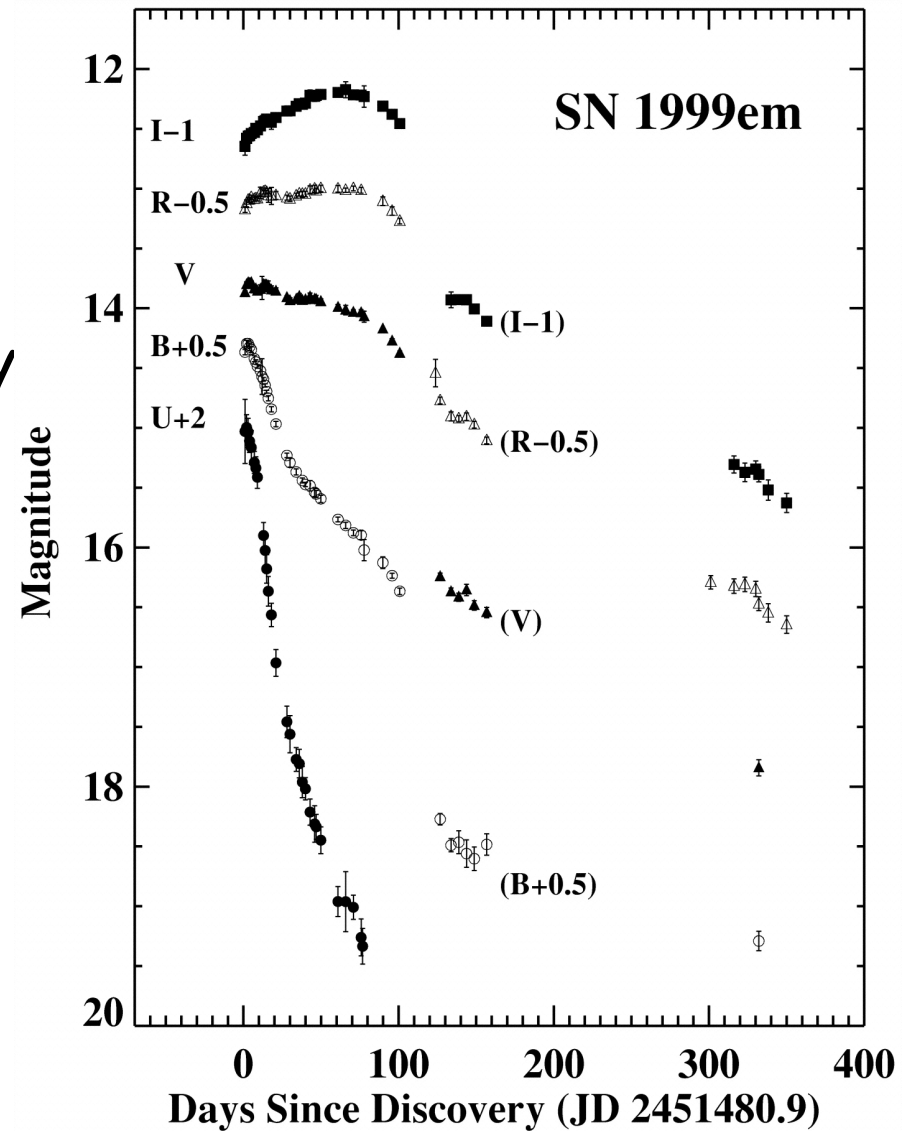
# Plateau phase

$R_0 \sim 10^{14}$  cm  $\Rightarrow$  adiabatic expansion

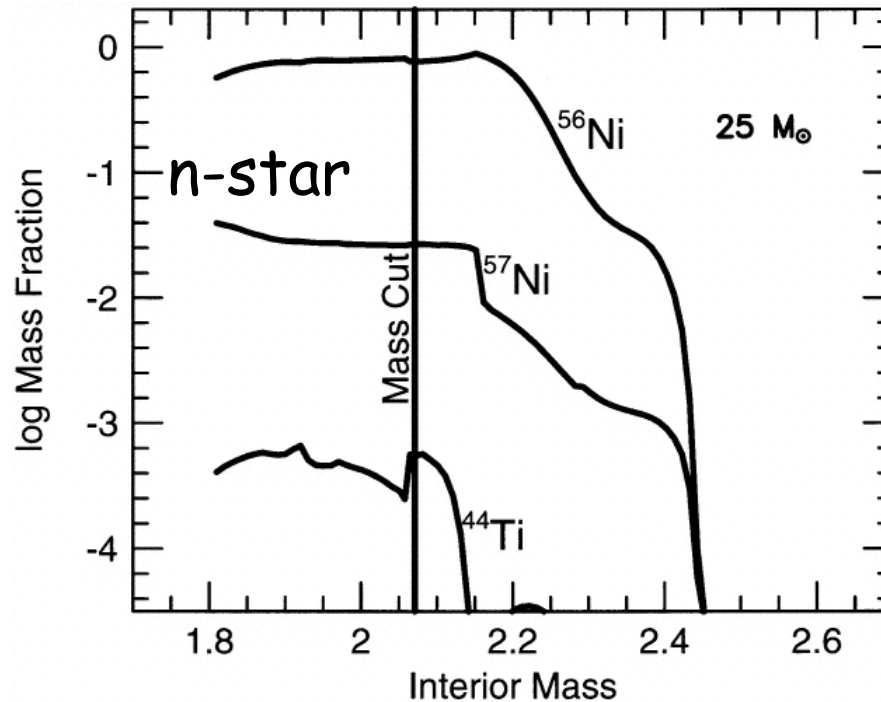
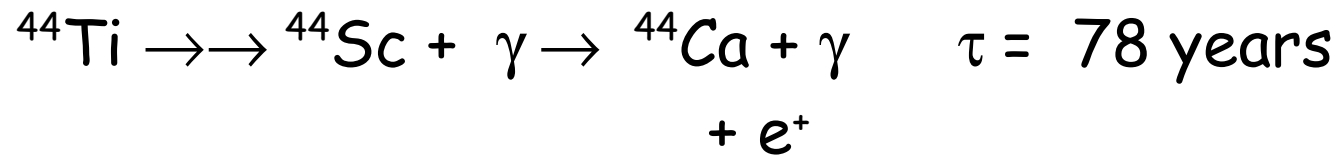
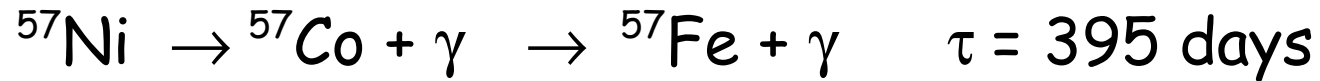
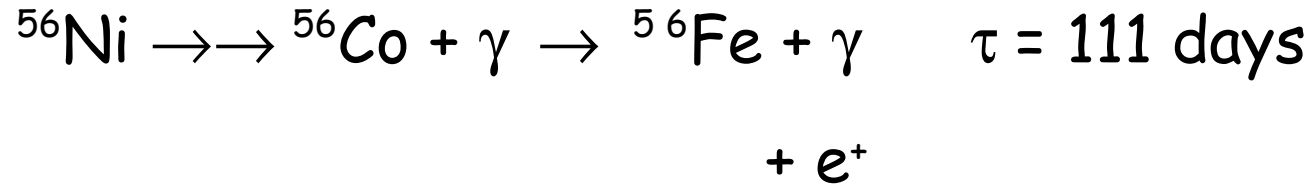
not important

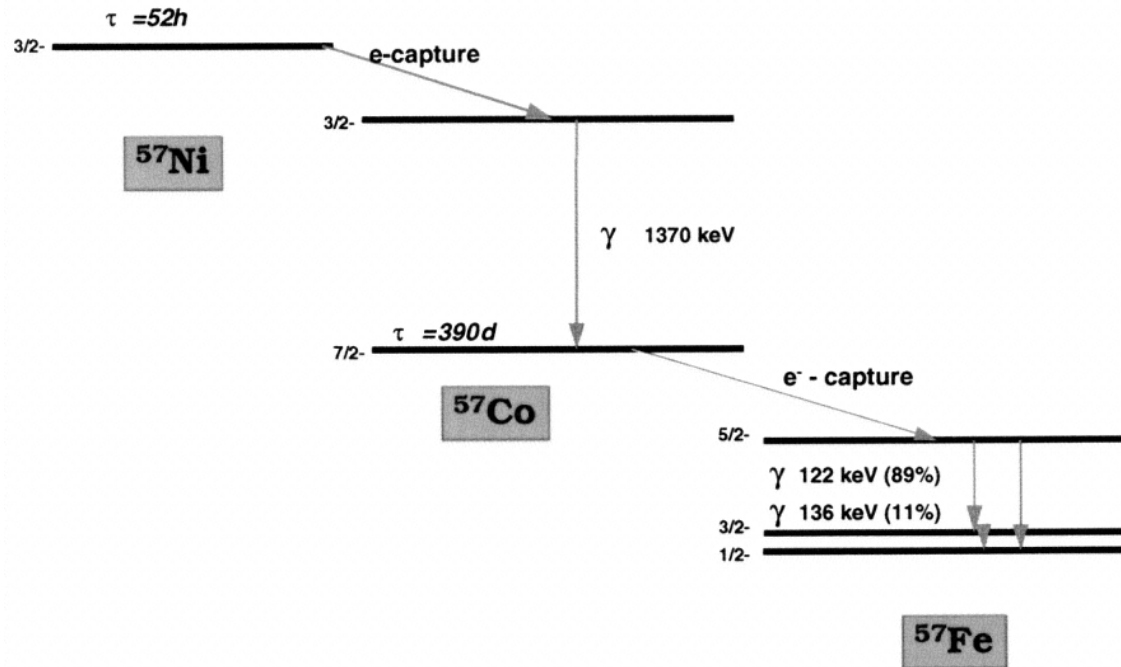
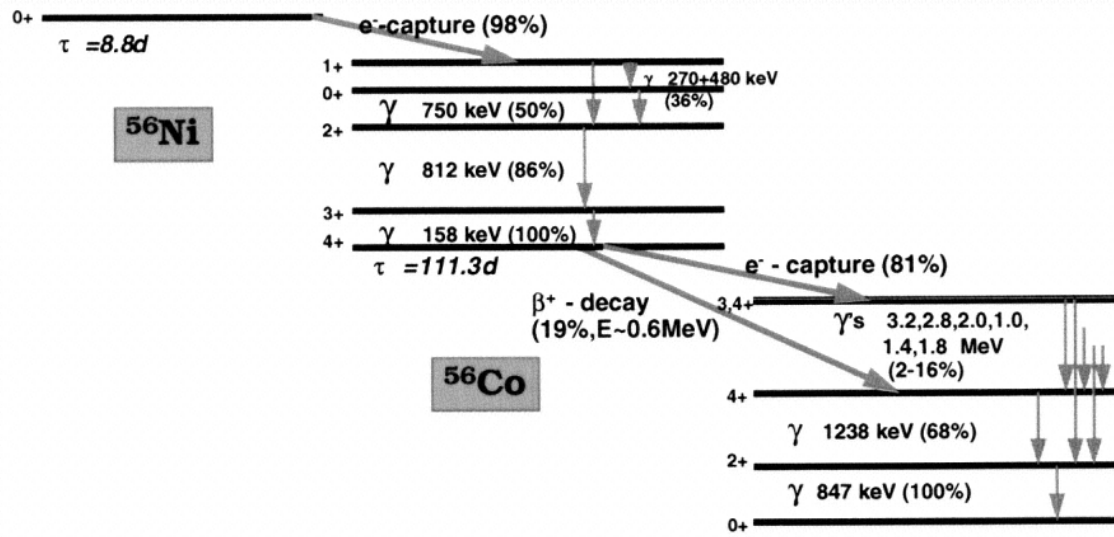
$\Rightarrow$  diffusive release of shock energy

$\tau_{\text{diff}} \sim 100$  days  $\Rightarrow$  plateau



# Radioactivity

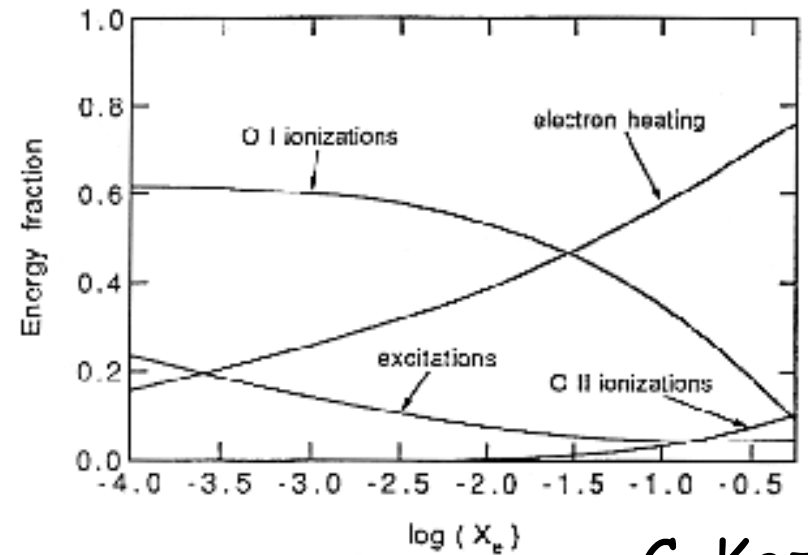
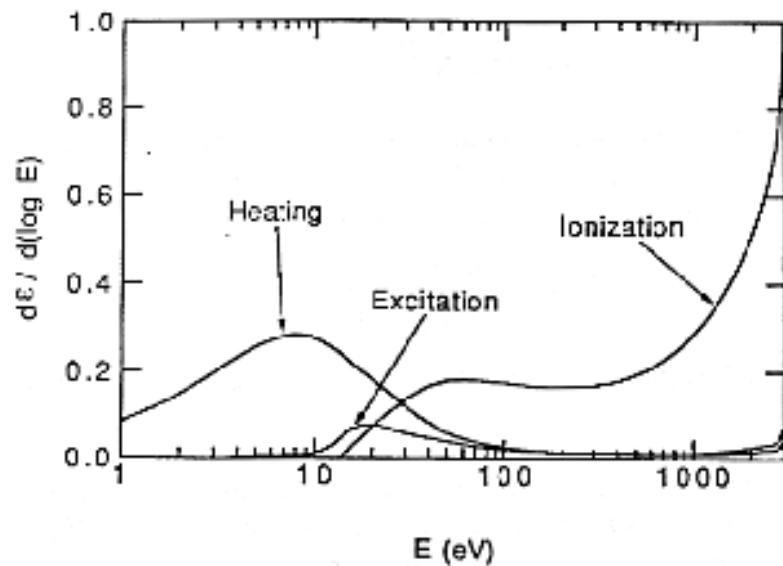






# Gamma-ray thermalization

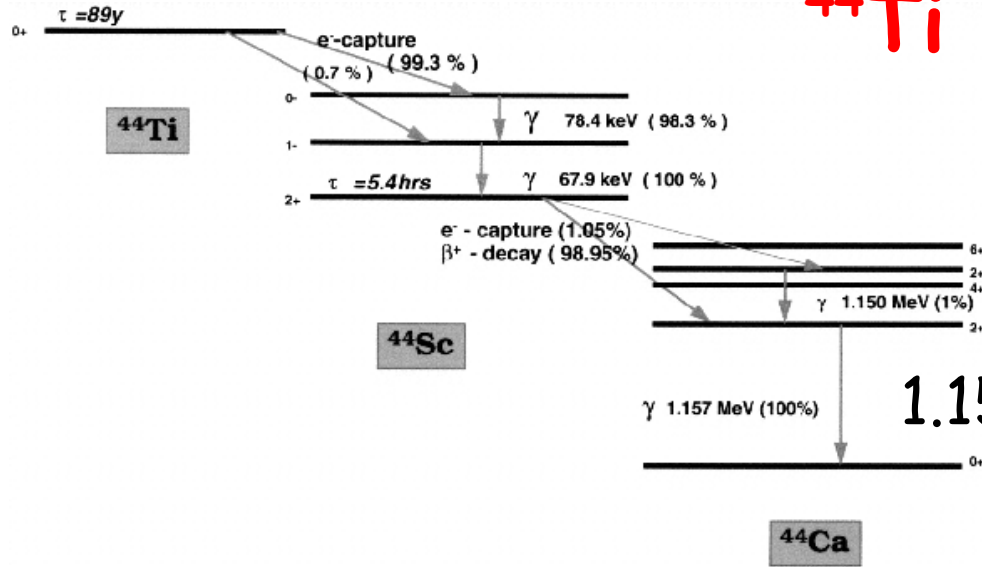
Gamma-rays  $\rightarrow$  non-thermal electrons (10 eV - 100 keV)  
non-thermal electrons  $\rightarrow$  ionizations, excitations, heating  
ionizations  $\rightarrow$  recombinations, excitations  $\rightarrow$  rad. decays,  
heating  $\rightarrow$  coll. excit.  $\rightarrow$  rad. decays



C. Kozma

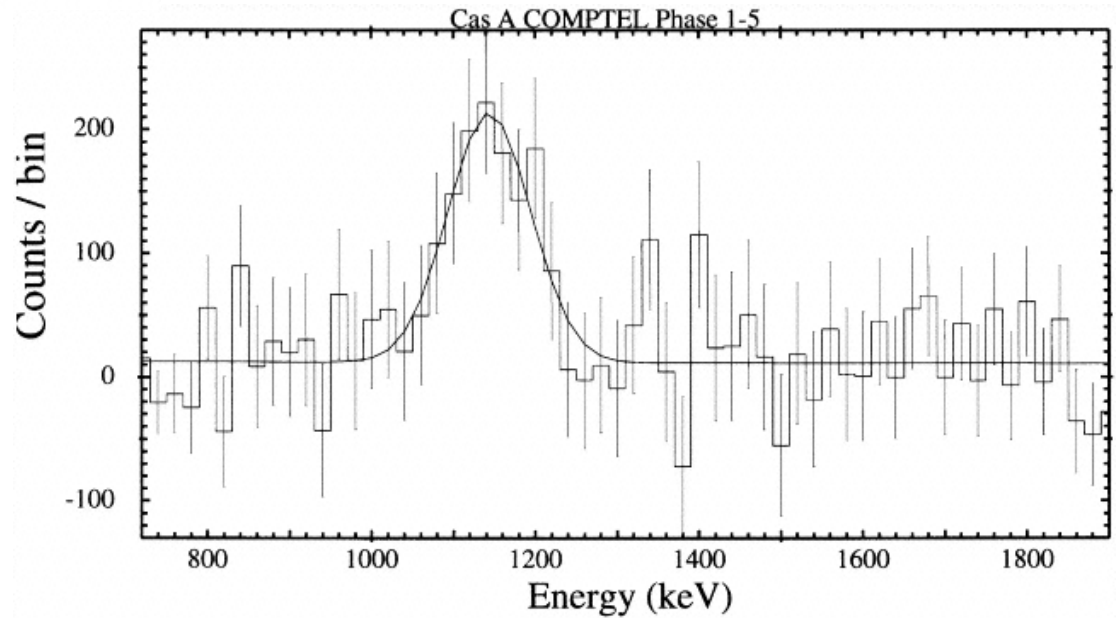
Gamma-rays thermalized to UV/optical/IR photons

# $^{44}\text{Ti}$ decay



1.157 MeV

Cas A



# Radioactivity



$$\tau = 8.8 \text{ days} \quad \tau = 111 \text{ days}$$

Gammas

$$L_\gamma = 1.27 \times 10^{42} \left( \frac{M({}^{56}\text{Ni})}{0.1 M_{\text{sun}}} \right) e^{-t/111.3 d}$$

positrons

$$L_+ = 4.44 \times 10^{40} \left( \frac{M({}^{56}\text{Ni})}{0.1 M_{\text{sun}}} \right) e^{-t/111.3 d}$$

positrons trapped (large cross section)

gammas scattered

$$L_{\text{bol}} = L_\gamma [(1 - e^{-\tau_\gamma}) + 0.035] \text{ erg s}^{-1}$$

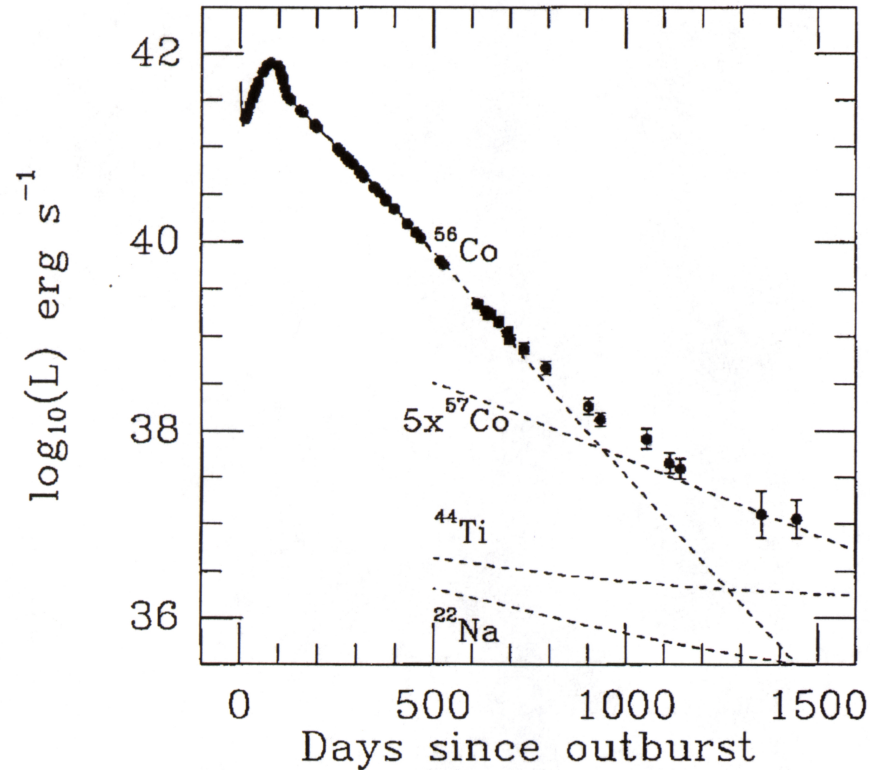
$$\tau_\gamma = \kappa_\gamma \rho R = \kappa_\gamma \frac{3}{4\pi} \frac{M}{V^2 t^2} = 0.38 \frac{Z}{A} \left( \frac{M}{M_{\text{sun}}} \right) \left( \frac{V}{10^4 \text{ km s}^{-1}} \right)^{-2} \left( \frac{t}{100 \text{ days}} \right)^{-2}$$

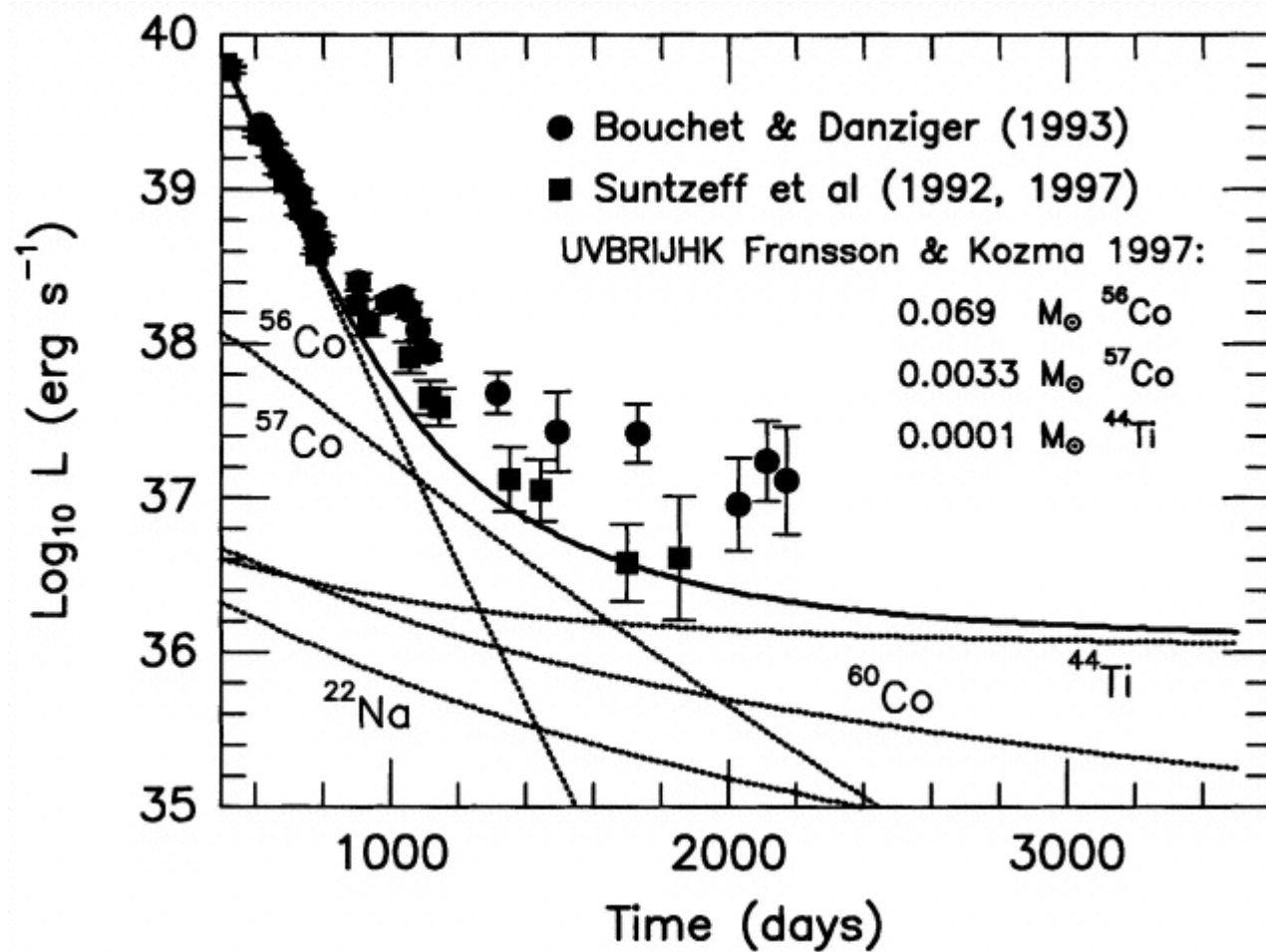
SN 1987A

$$M_{core} \approx 4 M_{sun} \quad V_{core} \approx 2000 \text{ km s}^{-1}$$

$$\tau_y \approx 40 \left( \frac{t}{100 \text{ days}} \right)^{-2}$$

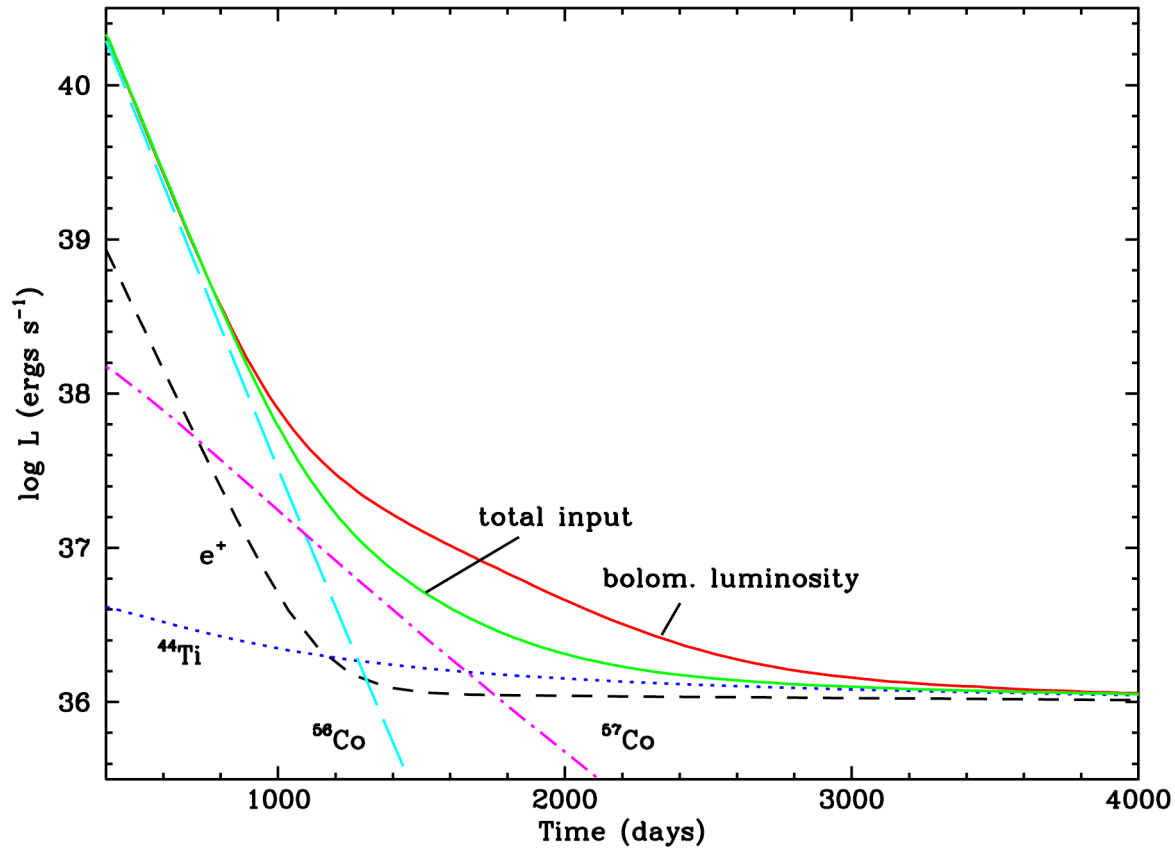
$$M_{bol} = -t \frac{2.5 \log e}{11.3 \text{ days}} + const = -\frac{t}{102.5 \text{ days}} + const$$





# SN 1987A radioactivities

C. Kozma + CF



$$M(^{56}\text{Ni}) = 0.07 M_{\odot}, M(^{57}\text{Ni}) = 3 \times 10^{-3} M_{\odot}, M(^{44}\text{Ti}) = 1 \times 10^{-4} M_{\odot}$$



# Sobolev approximation

$$\frac{v - v_0}{v_0} = \frac{V_z}{c} = \frac{z}{r} V \frac{r}{c} = \text{constant}$$

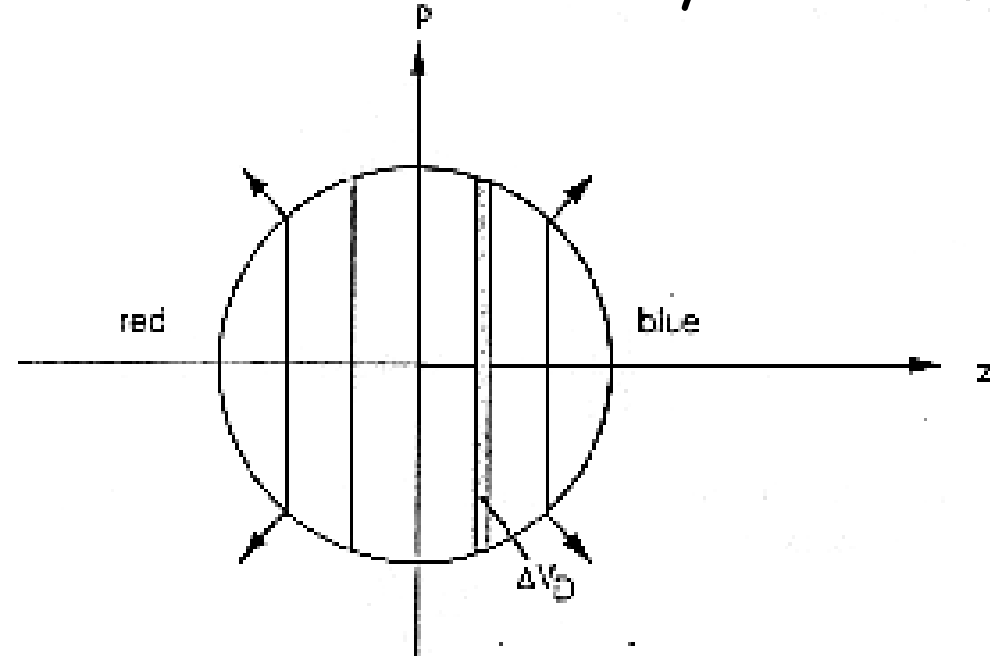
Homologous exp.  $V(r) = V_0 \frac{r}{R_0} = \frac{r}{t}$

$$\frac{z}{R_0} = \frac{ct}{R_0} \frac{(v - v_0)}{v_0}$$

$$\tau_v = \sigma_v n_1 \delta l$$

$$\sigma_v = \frac{\pi e^2}{mc} \frac{f_{12}}{\Delta v_D}$$

constant velocity surface



$$\delta l = \frac{\partial r}{\partial V} \Delta V_D = \left[ \frac{\partial}{\partial r} \left( \frac{V_0}{R_0} r \right) \right]^{-1} \Delta V_D = \frac{R_0}{V_0} \Delta V_D = \frac{\Delta v_D}{v} ct$$

$$\tau = \frac{A_{21} \lambda^3 g_2}{8 \pi g_1} \left( n_1 - \frac{g_1}{g_2} n_2 \right) t.$$

= Sobolev approx

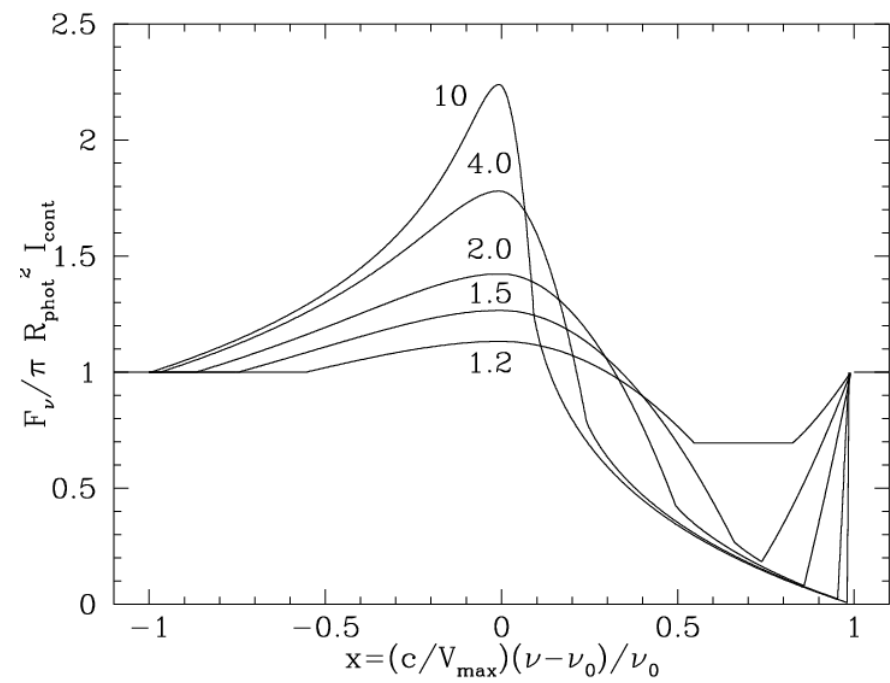
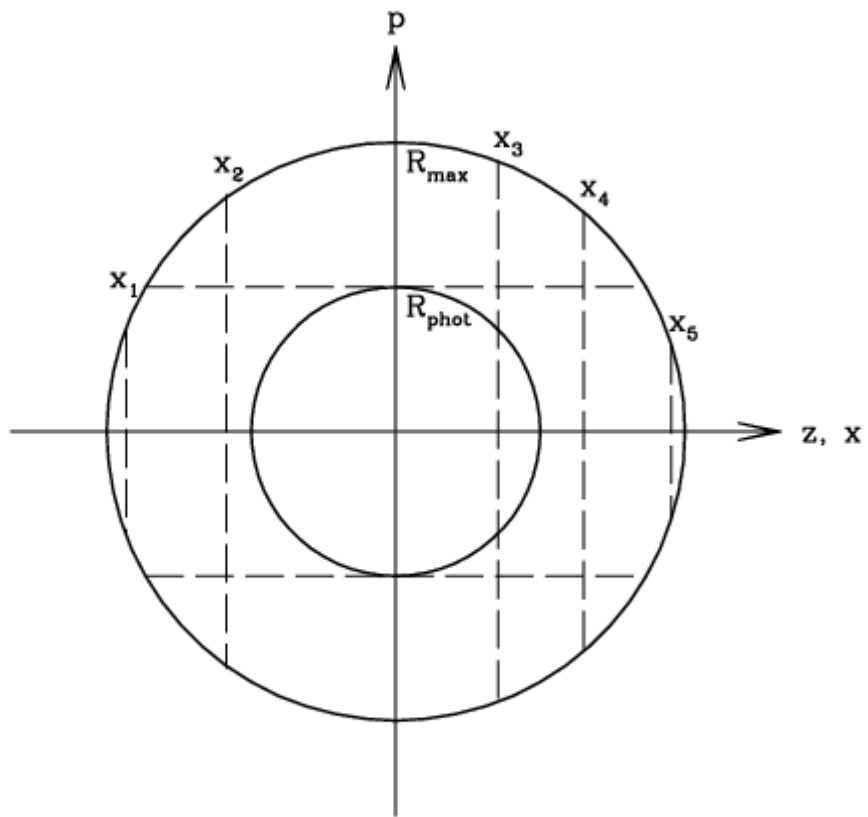
$$\beta = \frac{1}{2} \tau \int_0^\tau \int_{-1}^1 e^{-\tau'} d\mu d\tau' = \frac{1 - e^{-\tau}}{\tau}.$$

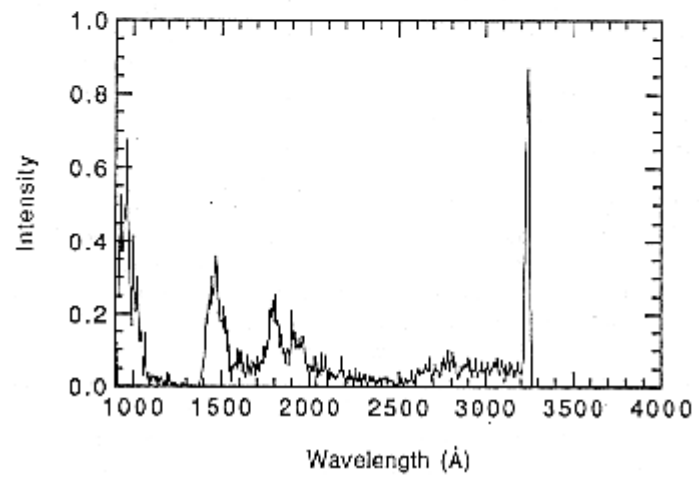
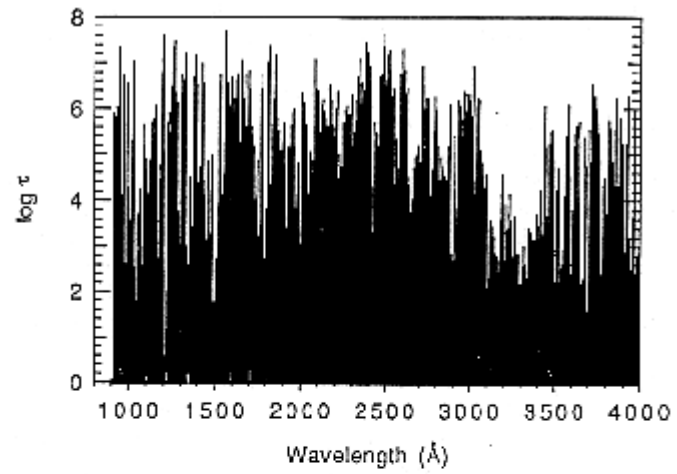
$$S = \frac{2 h \nu^3}{c^2 (n_2 g_1 / n_1 g_2 - 1)}$$

$$F_x = 2 \pi \int_{p_{min}}^{p_{max}} [S(p, z = xR)(1 - e^{-\tau}) + e^{-\tau} I_{cont}] p dp$$

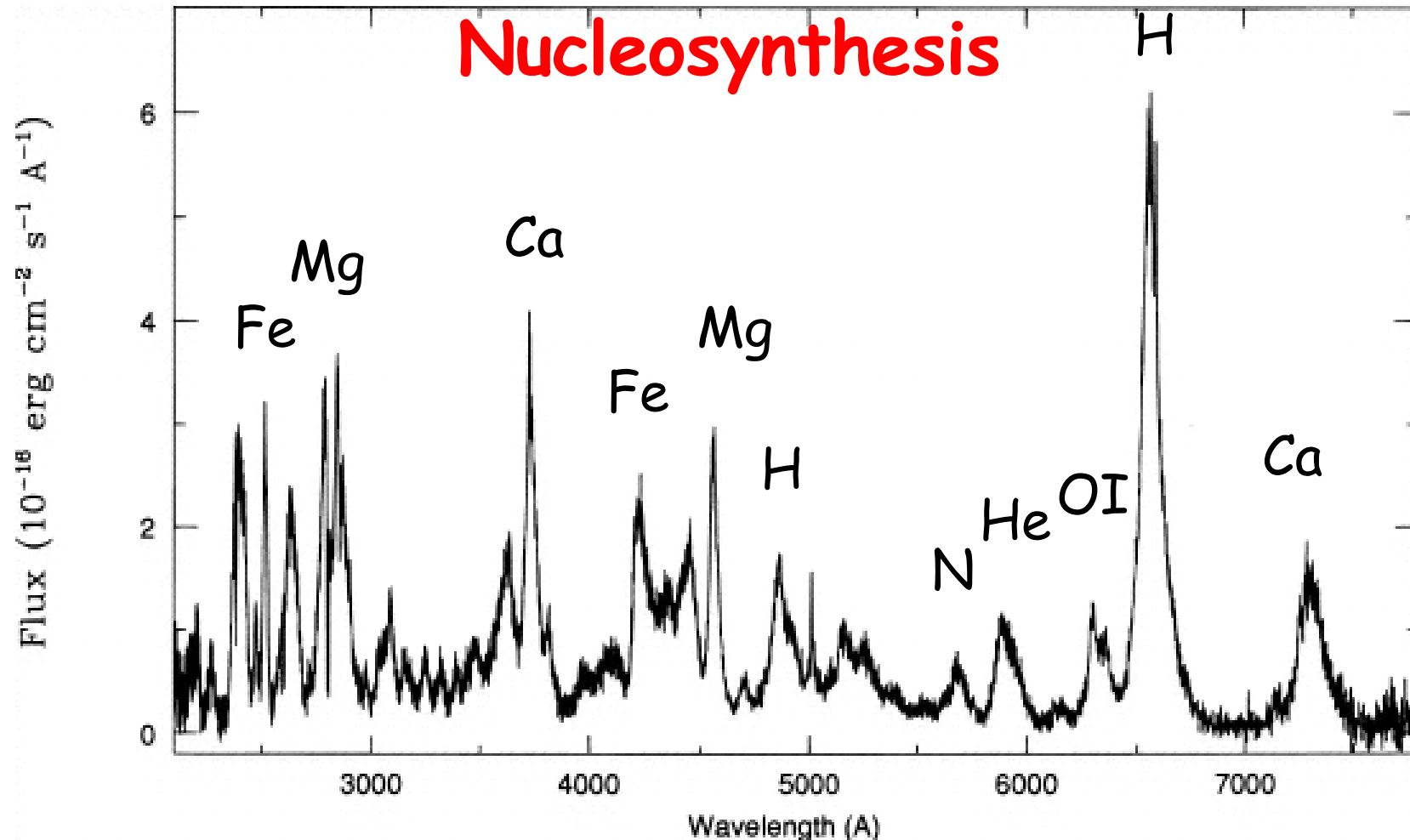
$$p dp = r dr \quad \text{for constant } z \quad (\text{i.e., constant } x)$$

$$F_x = 2 \pi \int_{r_{min}}^R [S(r)(1 - e^{-\tau}) + e^{-\tau} I_{cont}] r dr$$





# Nucleosynthesis



H	$7.2 \pm 2$	He	5.8	$M_{\text{initial}} \sim 20 M_{\odot}$
N	$3.4 \times 10^{-2}$	O	$1.9 \pm 1$	
Ne	$6.0 \times 10^{-2}$	Mg	$2.2 \times 10^{-2}$	
$^{44}\text{Ti} (\rightarrow ^{44}\text{Ca})$	$1.0 \times 10^{-4}$	$^{56}\text{Ni} (\rightarrow ^{57}\text{Fe})$	0.07	
$^{57}\text{Ni} (\rightarrow ^{57}\text{Fe})$	$3 \times 10^{-3}$	$^{58}\text{Ni} + ^{60}\text{Ni}$	$6.0 \times 10^{-3}$	

C. Kozma + CF 2002

$$F_x = 2\pi \int_{r_{min}}^R [S(r)(1 - e^{-\tau}) + e^{-\tau} I_{cont}] r dr$$

$$S = \frac{(1 - \epsilon)\beta W I_{rm cont} + \epsilon B_v}{(1 - \epsilon)\beta + \epsilon}$$

$$W(r) = \frac{1}{2} [1 - \sqrt{1 - (R_{phot}/r)^2}]$$